

Figure 1: Various structural image representations modelled as undirected graphs

Image Classification:

the process of assigning a given image into one of several predefined categories.

1. Project Aims

- Exploit the patterns and relationships between regions by representing images as undirected graphs.
- Employ the recently-proposed Graph Neural Networks [1] model to handle the classification of structured data:

2. Image Structure as Graphs

An image's structural context can be represented as a graph $G=\{N, E\}$, where N (nodes) correspond to interest regions and E (edges) correspond to the connections between two distinct regions. Figure 1 illustrates the structural representations considered.

Region Adjacency Graph (RAG):

- Segment regions based on colour and texture using Edge Flow [2].
- Fit ellipses and connect adjacent regions.

Grid structure:

- Dense sample every 16th pixel, offsetting by half every odd row.
- Join NSEW neighbours where available.

Minimum Spanning Tree (MST):

- Detect regions with scale-invariant blob detector, Hessian-Laplace [3]. Identifies around 200-3000 regions per image.
- MST incurs the lowest total cost in forming a connected path to all nodes.

Delaunay Triangulation:

- Same interest regions as MST.
- Delaunay triangulation for a set P of points is a triangulation such that no point in P is inside the circumcircle of any triangle

3. Node and Edge Labels

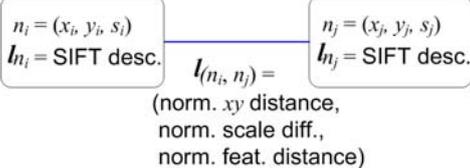


Figure 2: Node and edge information diagram

n is a node with center co-ordinates (x, y) and detected at scale s .

l_n is a node label and $l_{(n,m)}$ is an edge label.

SIFT = Scale Invariant Feature Transform [4] descriptor.

4. Filtering Nodes detected with Hessian-Laplace

- (1) Form a representative node set using k -means clustering in feature space. This is performed on a subset of images from the entire dataset.
- (2) Apply further heuristics to remove outliers and non-meaningful clusters.
- (3) For each image, associate all nodes to an appropriate cluster centroid.
- (4) Keep the node set in which each node is closest to its associated centroid. This yields a filtered node set containing at most k nodes.



Figure 3: Images before and after filtering Hessian-Laplace regions

5. Classification with Graph Neural Networks (GNN)

A state x_n is attached to node n , based on the information contained in the neighbourhood.

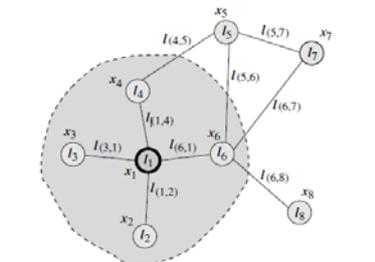


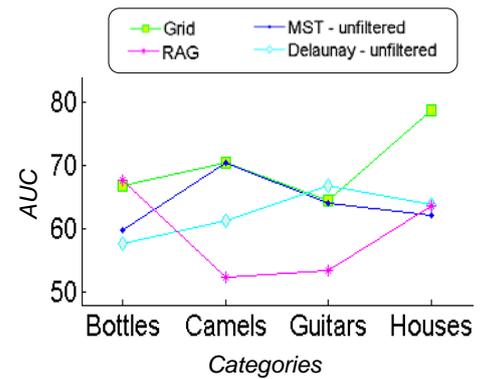
Figure 4: The state of node 1 (x_1) depends on its label (l_1), the labels of its edges ($l_{(1,n)}$), the states of neighbouring nodes ($x_{ne(i)}$) and their labels ($l_{ne(n)}$).

The node state contains a representation of the category and can be used to produce a decision output value o_n . At every iteration t , the state of $x_n(t+1)$ is calculated using some function f_w . Finally, the output o_n is calculated using another function g_w . In the GNN model, f_w and g_w are implemented by feedforward neural networks.

6. Results

We perform a repeated holdout on 350 images using the one-against-all approach.

GNN Structural Image Classification Performances



Ave AUC	RAG	Grid	MST Unfilt.	Delau Unfilt.	MST Filt.	Delau Filt.
	59.35	70.21	64.16	62.43	TBA	TBA

7. Future Work

- More features: invariant colour descriptors
- Combine various local invariant detectors to form a more representative set of regions
- Evaluate on a larger dataset with more image categories
- Better centroid proposals and try other clustering techniques: hierarchical k-means.
- More complex graph structures

8. References

- [1] Scarselli, F., Gori, M., Tsoi, A. C., Hagenbuchner, M., and Monfardini, G. The graph neural network model. *IEEE Transactions on Neural Networks*, 20(1):61–80, 2009.
- [2] Ma, W.-Y. and Manjunath, B. Edgeflow: a technique for boundary detection and image segmentation. *IEEE Transactions on Image Processing*, 9(8):1375–1388, August 2000.
- [3] Mikolajczyk, K. and Schmid, C. Scale & affine invariant interest point detectors. *International Journal on Computer Vision*, 60(1):63–86, 2004.
- [4] Lowe, D. G. Distinctive image features from scale-invariant keypoints. *International Journal on Computer Vision*, 60(2):91–110, 2004.